





# Quantum Supremacy: Checking a Quantum Computer with a Classical Supercomputer

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# The Quantum Space Race

Hardware Challenges:  
Quantity  
Quality



# Quantum Data



$$|0\rangle + |1\rangle$$



# Quantum Data



$$(|0\rangle + |1\rangle)^2 = |00\rangle + |01\rangle + |10\rangle + |11\rangle$$

# Really Big Data

$$(|0\rangle + |1\rangle)^n$$

n=50: supercomputer

n=300: more states than  
atoms in universe



# Bits and Qubits

Classical bit:

0 or 1

Coin on table

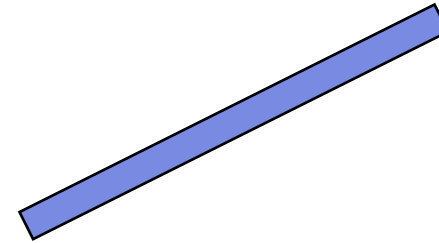


Digital: self-correcting

Quantum bit:

$$\psi = \cos\theta |0\rangle + \sin\theta e^{i\phi} |1\rangle$$

Coin in space

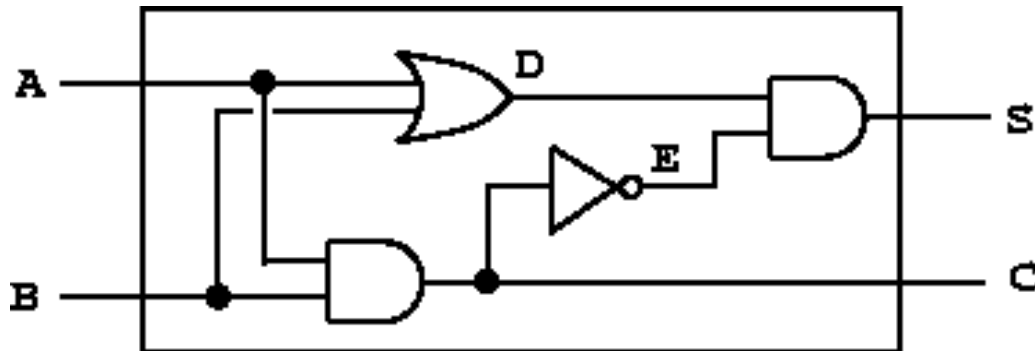


Analog: sensitive to small errors

# Any Logic Built from Universal Gates

Classical circuit:

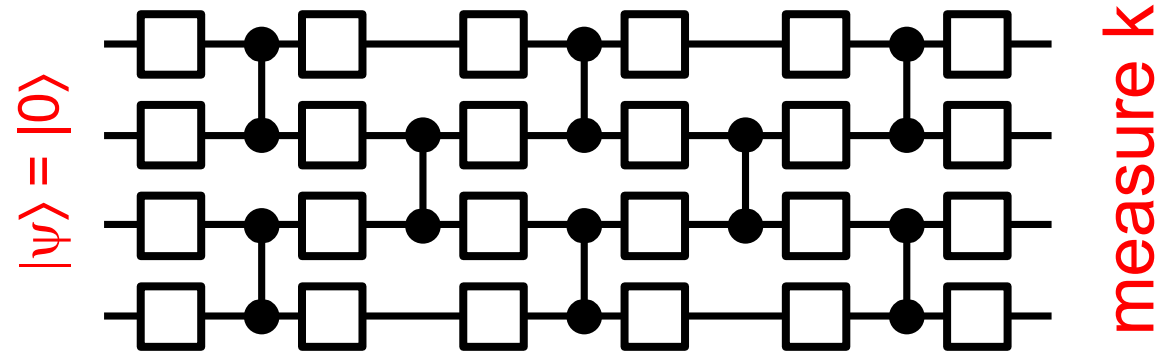
1 bit NOT  
2 bit AND  
Wiring fan-out



———— Space (layout) —————>

Quantum circuit:

1 qubit rotation  
2 qubit CNOT  
-No copy-



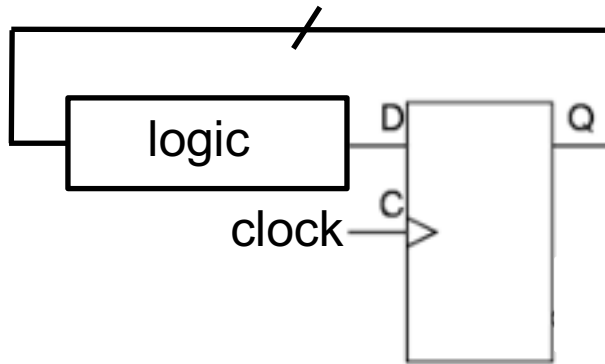
———— Time (sequence) —————>



# Full Digital (Clocked) Logic

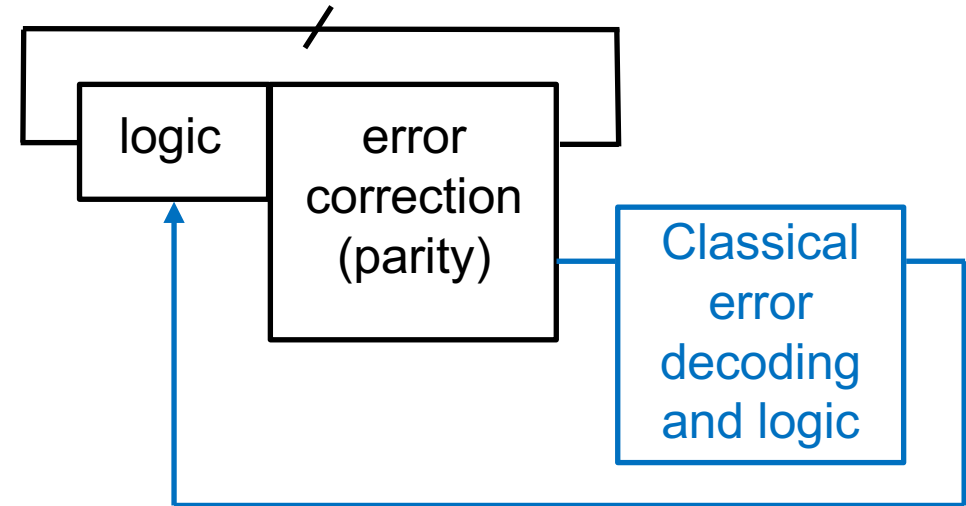
## Classical system:

D flip-flop aligns timing to clock



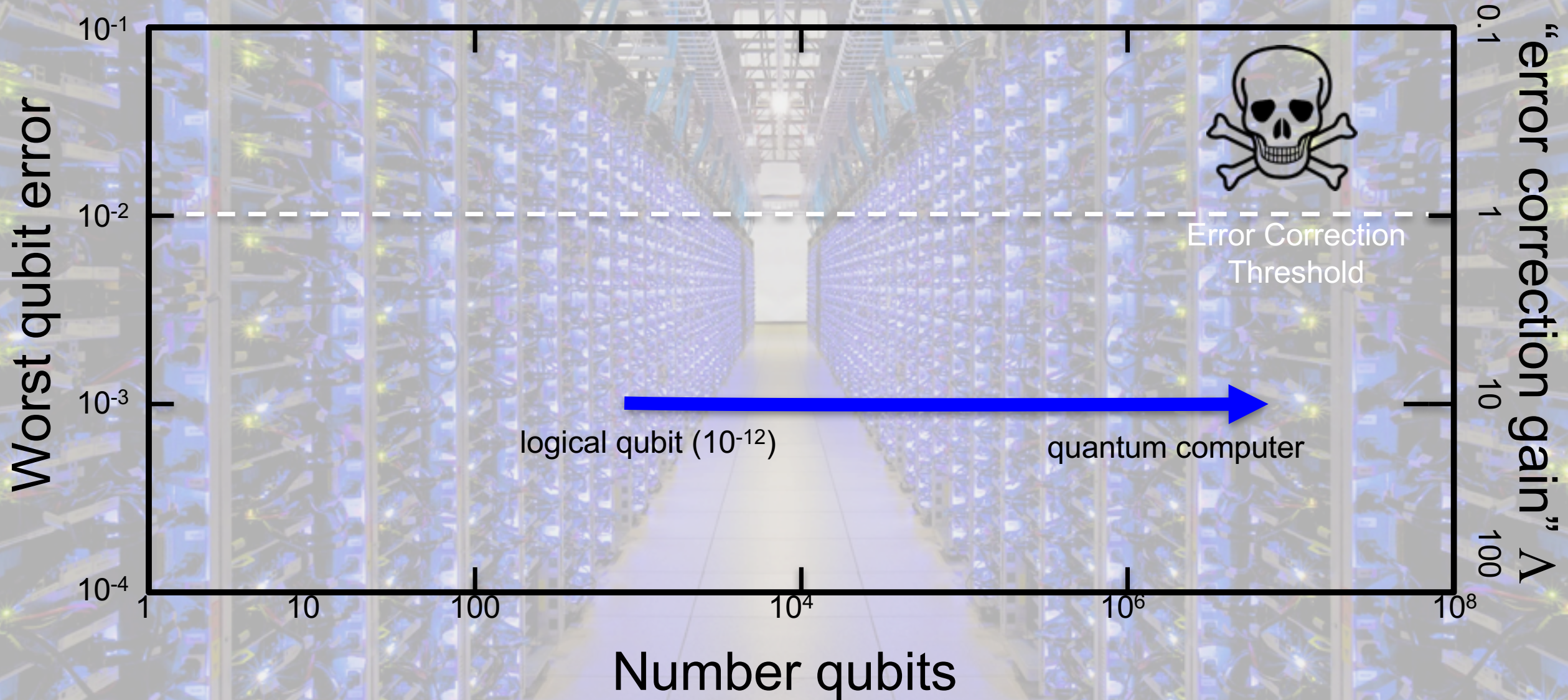
## Quantum system:

Error correction aligns amplitude and phase each round, makes “quantum flip-flop”



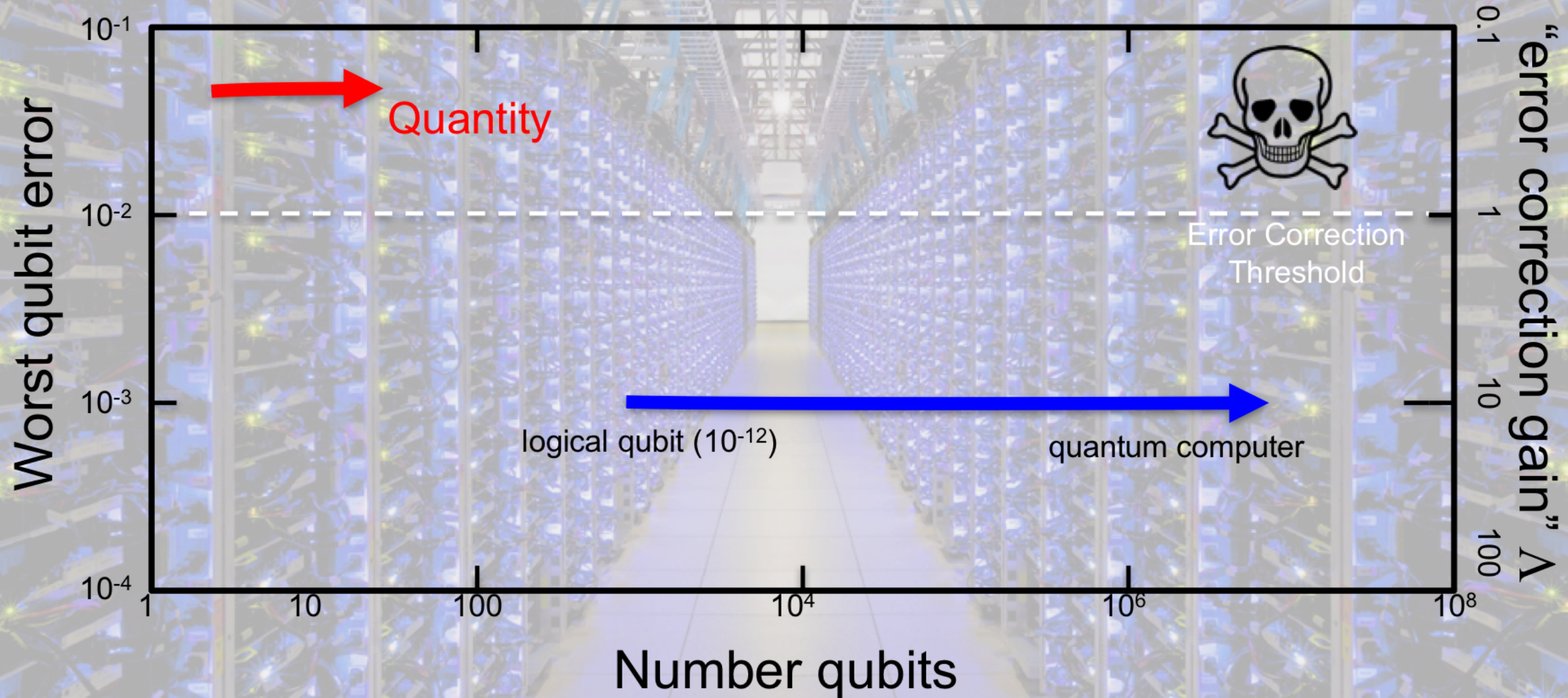
10<sup>-12</sup> errors: 1000 qubits + 0.1% errors

# Systems: Quantity and Quality



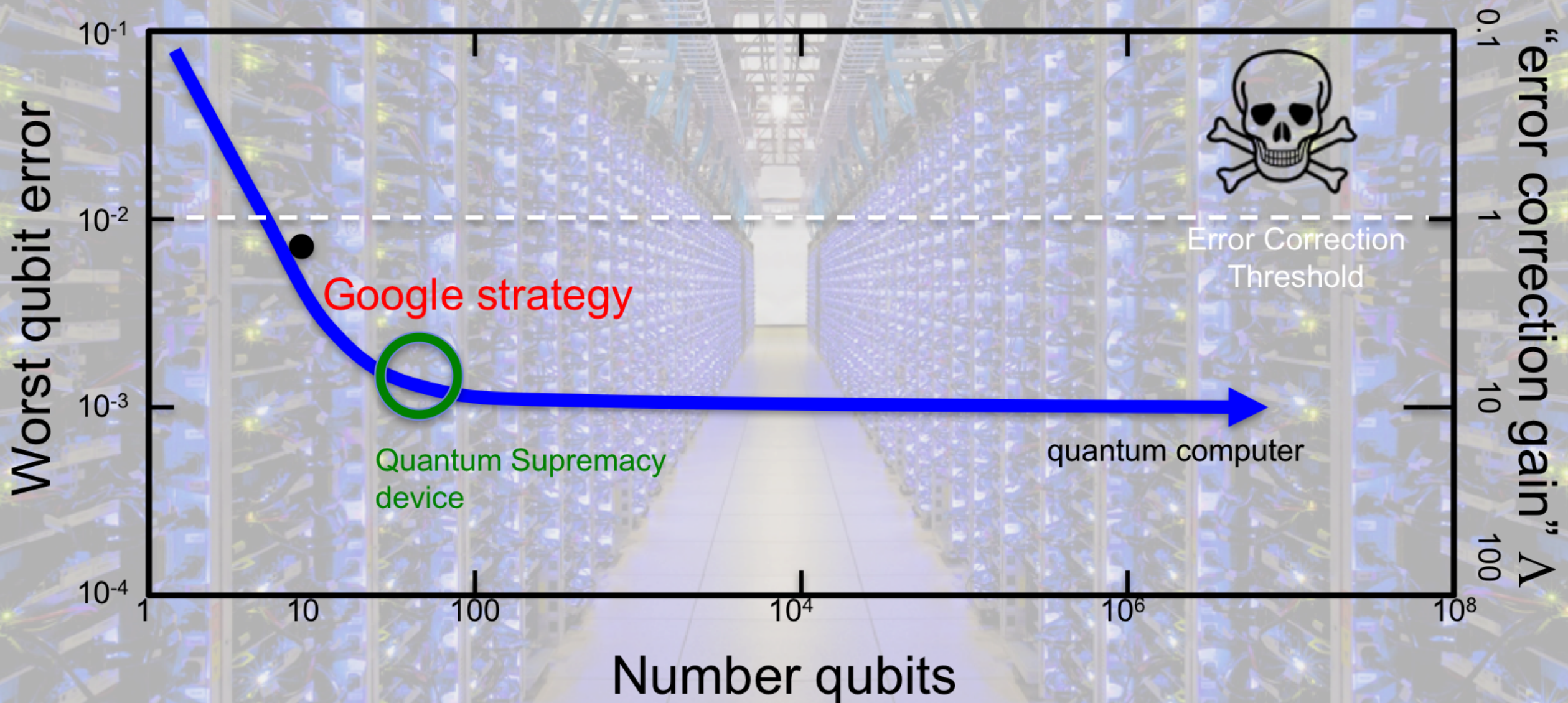


# Systems: Quantity and Quality



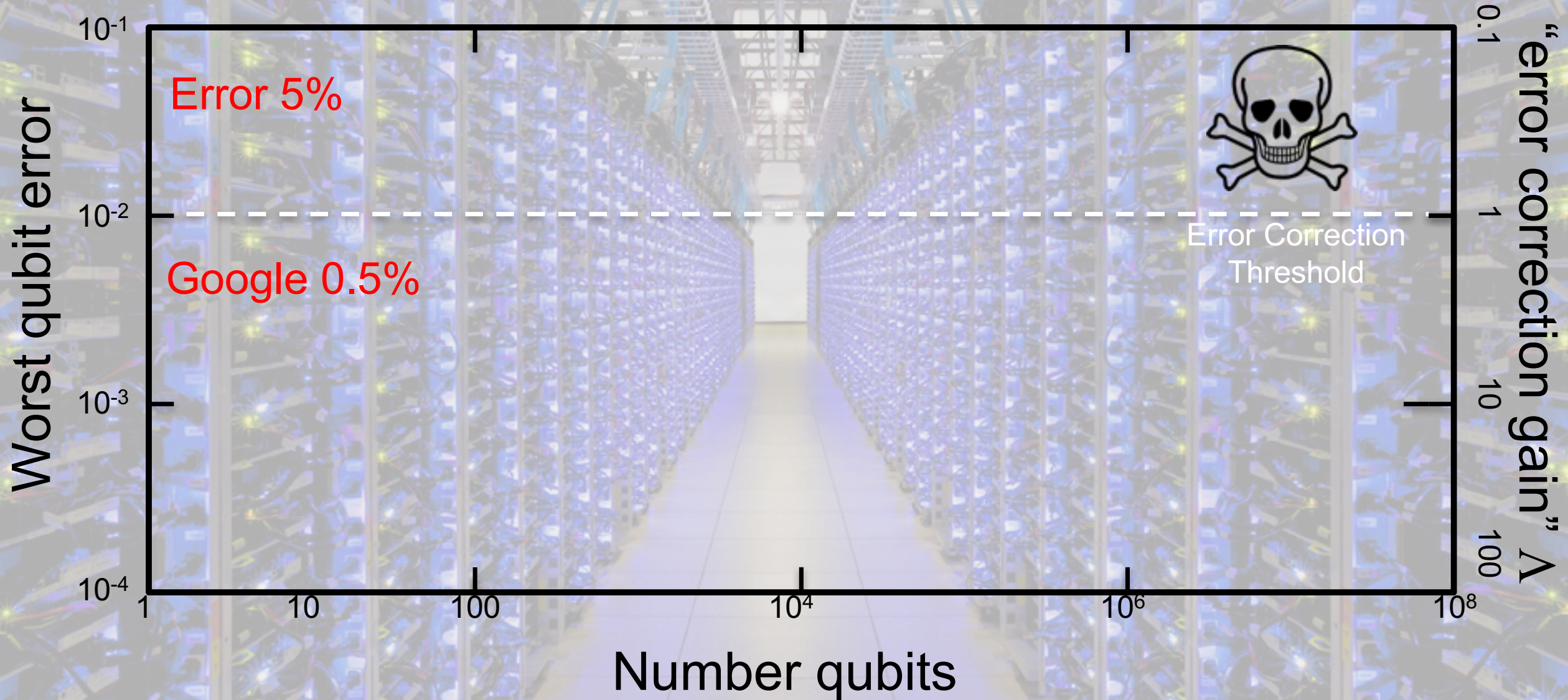


# Systems: Quantity and Quality



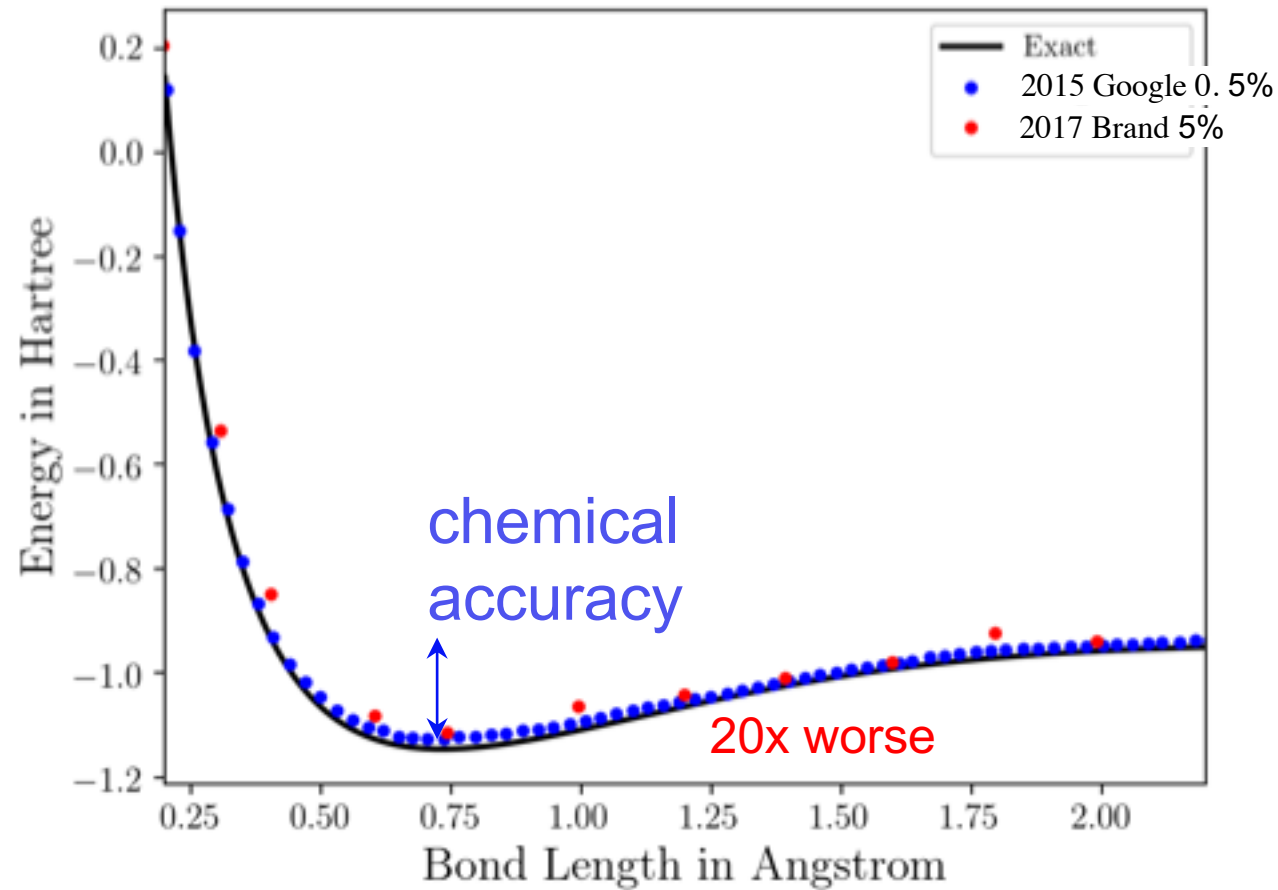


# Systems: Quantity and Quality

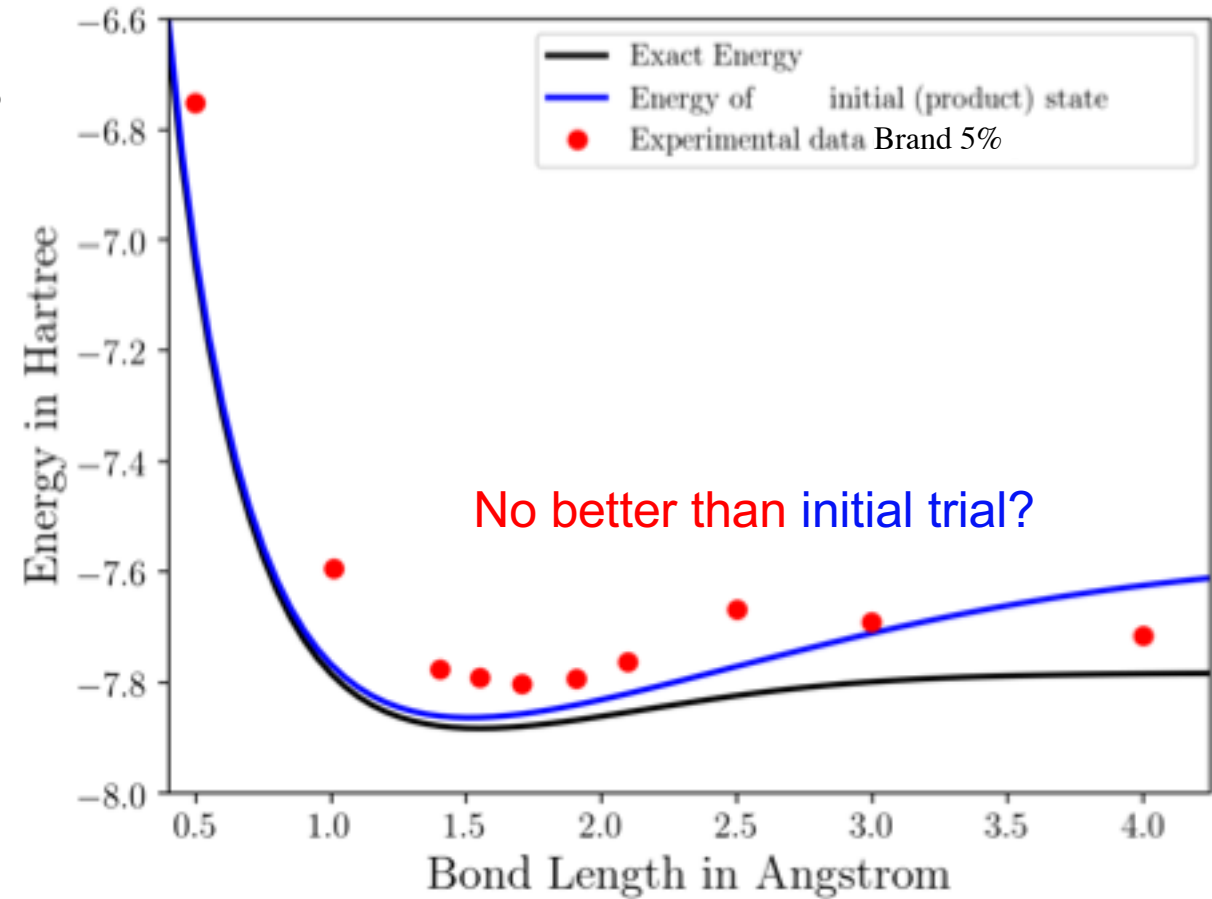


# Quality in Quantum Chemistry Experiments

## H<sub>2</sub> Molecule



## LiH Molecule



Quality:

- 1) Need low errors for accurate predictions
- 2) Need figure of merit for useful



# Quantum Supremacy

**Quantum Supremacy** (Preskill): for well defined problem, show more computation power for quantum computer



Cautions:

1) How know a hard problem?

50 qubits not necessarily computationally complex

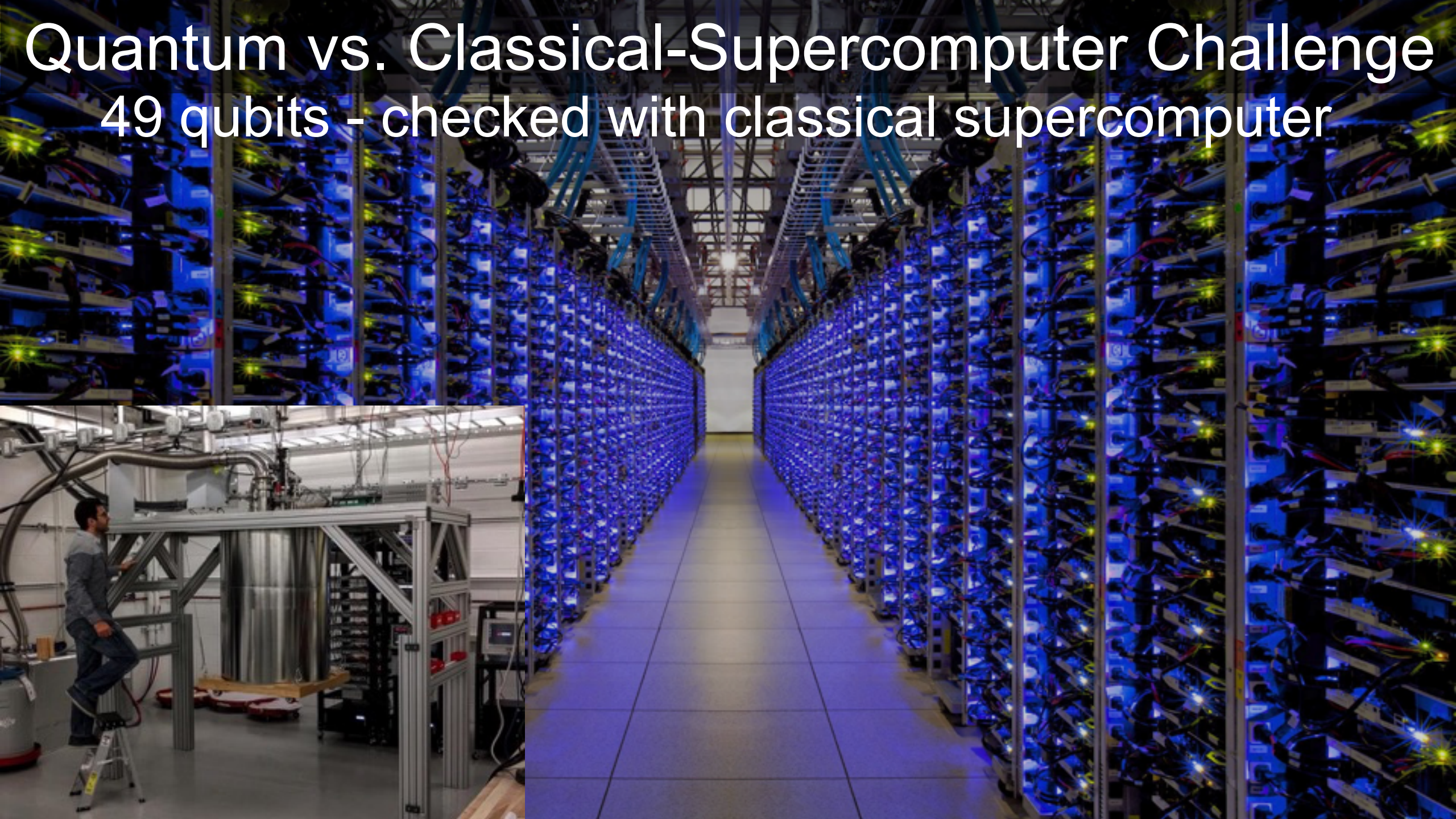
2) From example:

50 qubits with simple answer and without need for good control  
likely solvable by short computation

# Google: QS++

- 1) **Exponential:** demonstrate exponentially growing computation space
- 2) **Hard:** Unstructured problem, so provably hard (but not “useful”)
- 3) **Quality:** need low errors in qubit control, used to validate control
- 4) **Universal:** forward compatible to general purpose computer





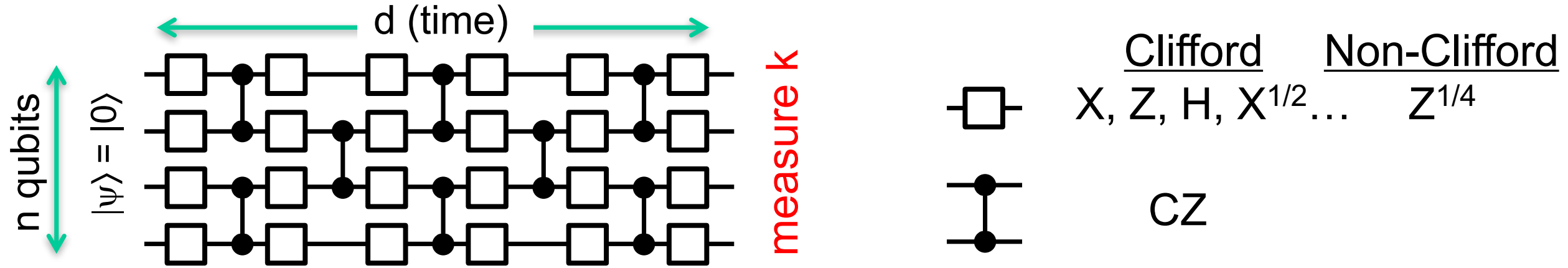
# Quantum vs. Classical-Supercomputer Challenge

49 qubits – checked with classical supercomputer



# Quantum Supremacy Algorithm: Qubit Speckle

1) Choose 1 instance, randomly from gateset



2) Run quantum computer, measure  $k$  ( $2^n$  possible outcomes)  
repeat sampling 100,000 times

1 s

(Random guess: any outcome  $k$  has probability  $p_{cl} = 1/2^n$ )

3) Calculate  $|\psi\rangle$ ,  $p(k) = |\langle k|\psi\rangle|^2$  store in lookup table

days  
200 drives

4) Correlation: cross entropy

$$S = \langle \ln p(k)/p_{cl} \rangle$$

5) Compare to theory

$$S_{qu} \cong 0.42 \quad \text{quantum}$$

6) Try another instance

$$S_{cl} \cong -0.58 \quad \text{classical}$$

speckle = coherence  
predict = fidelity

# Intrinsic Errors in Quantum Computation

$$S_{\text{tot}} \cong P_0 S_{\text{qu}} + (1 - P_0) S_{\text{cl}}$$

Probability of no error:

$$P_0 = \exp[-N_g \varepsilon_g]$$

Average number of errors:

$$N_g \varepsilon_g = 49 \times 7 \times 0.005 = 1.7$$

Need: Quantity with Quality

Windows

A fatal exception 0E has occurred at 0028:C562F1B7 in VXD ctpci9x(05) + 00001853. The current application will be terminated.

- Press any key to terminate the current application.
- Press CTRL+ALT+DEL again to restart your computer. You will lose any unsaved information in all applications.

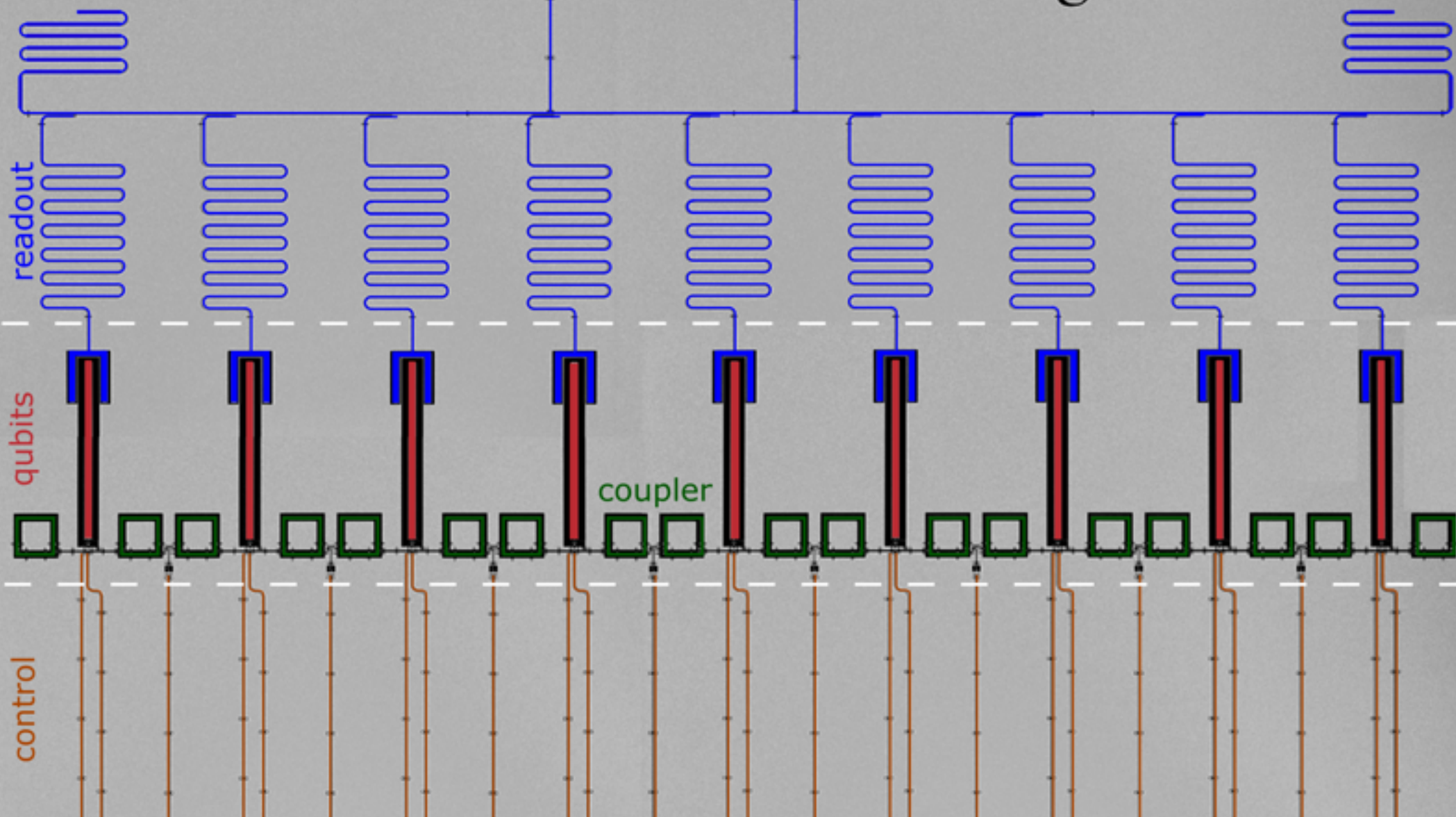
Press any key to continue \_



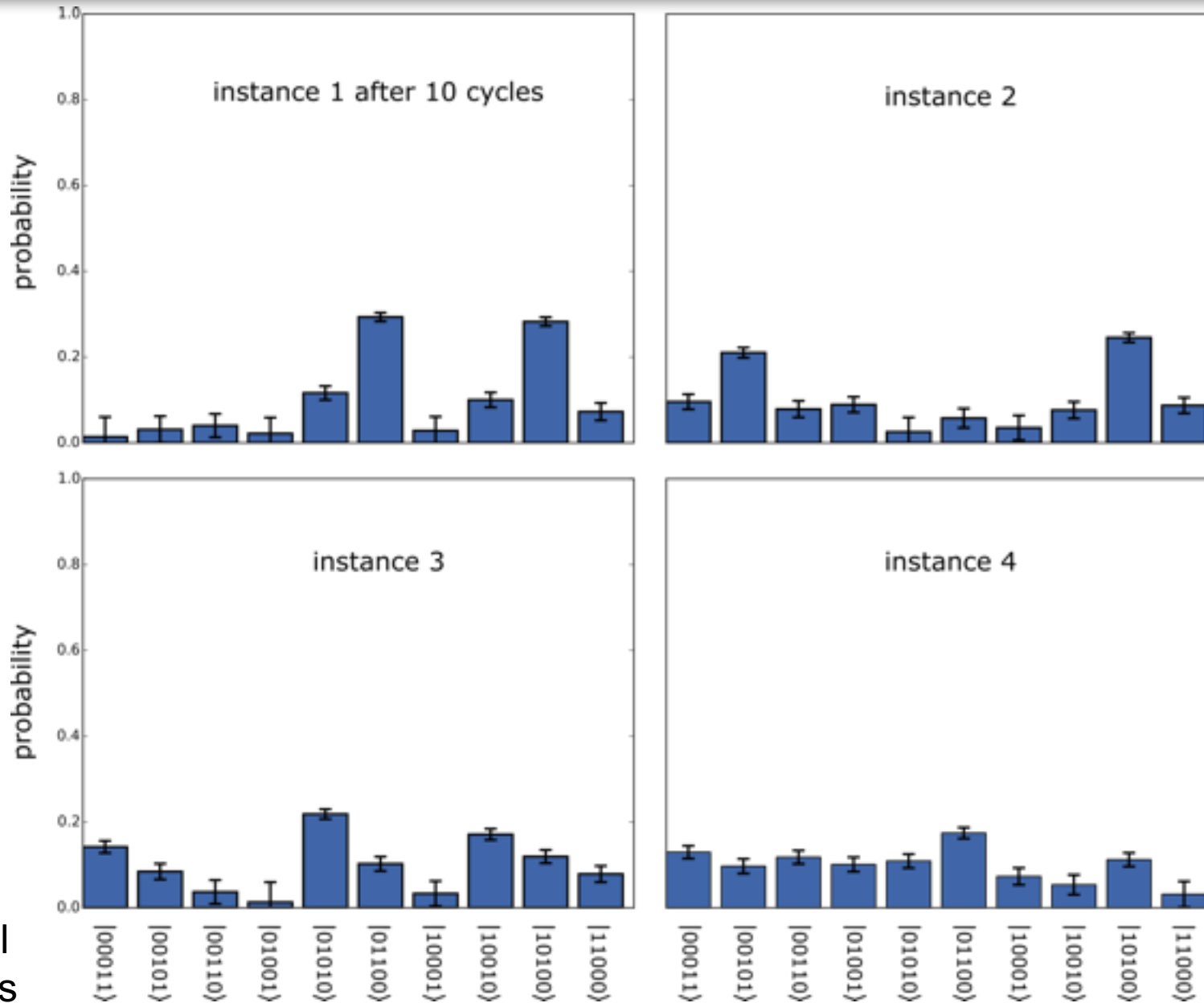
500  $\mu\text{m}$

UCSB

$\langle \text{Google} | e \rangle$



# Typical dataset with 5 qubits



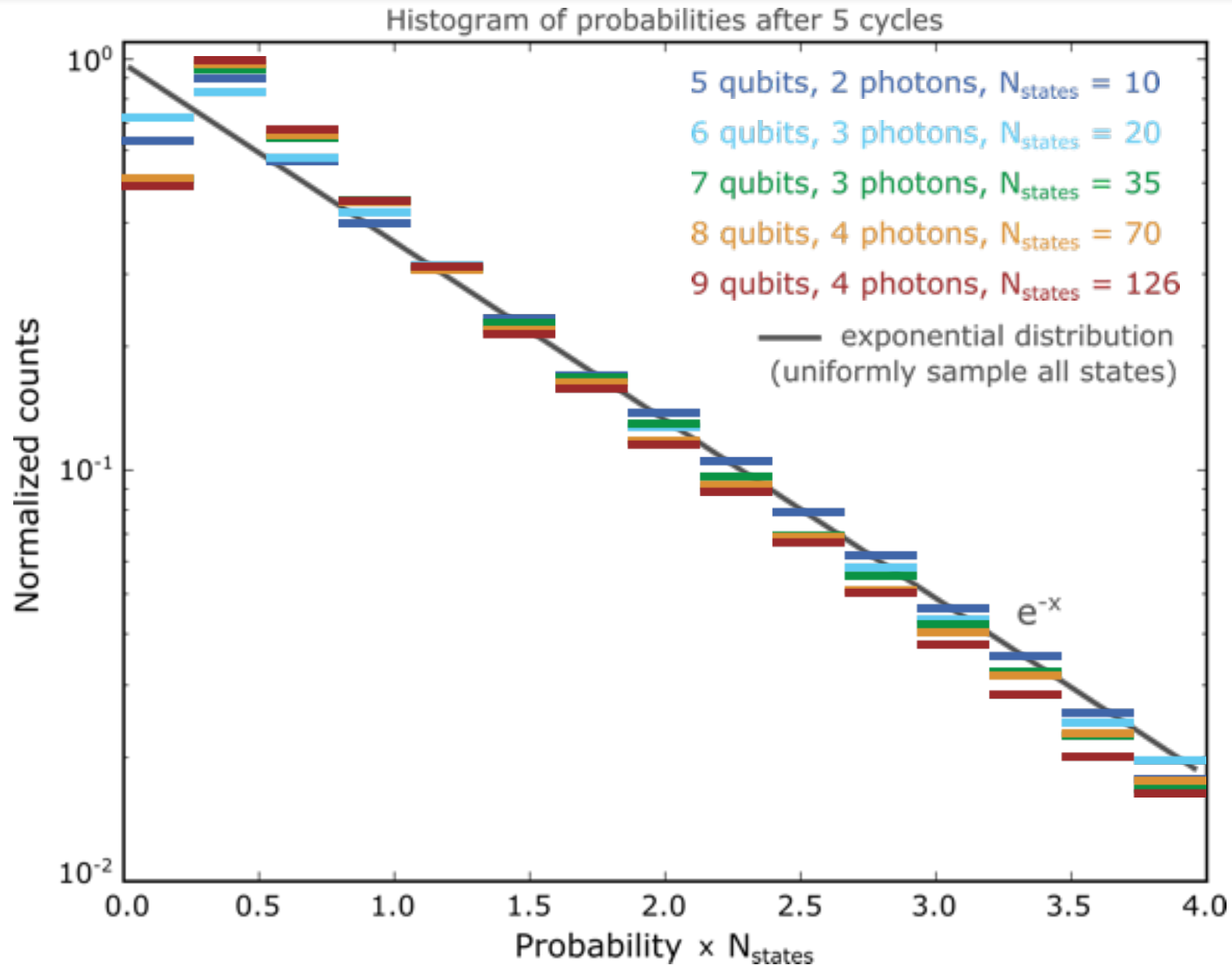
quantum info  
just from  
prob. histograms

statistical  
error bars

photon conserving  
states

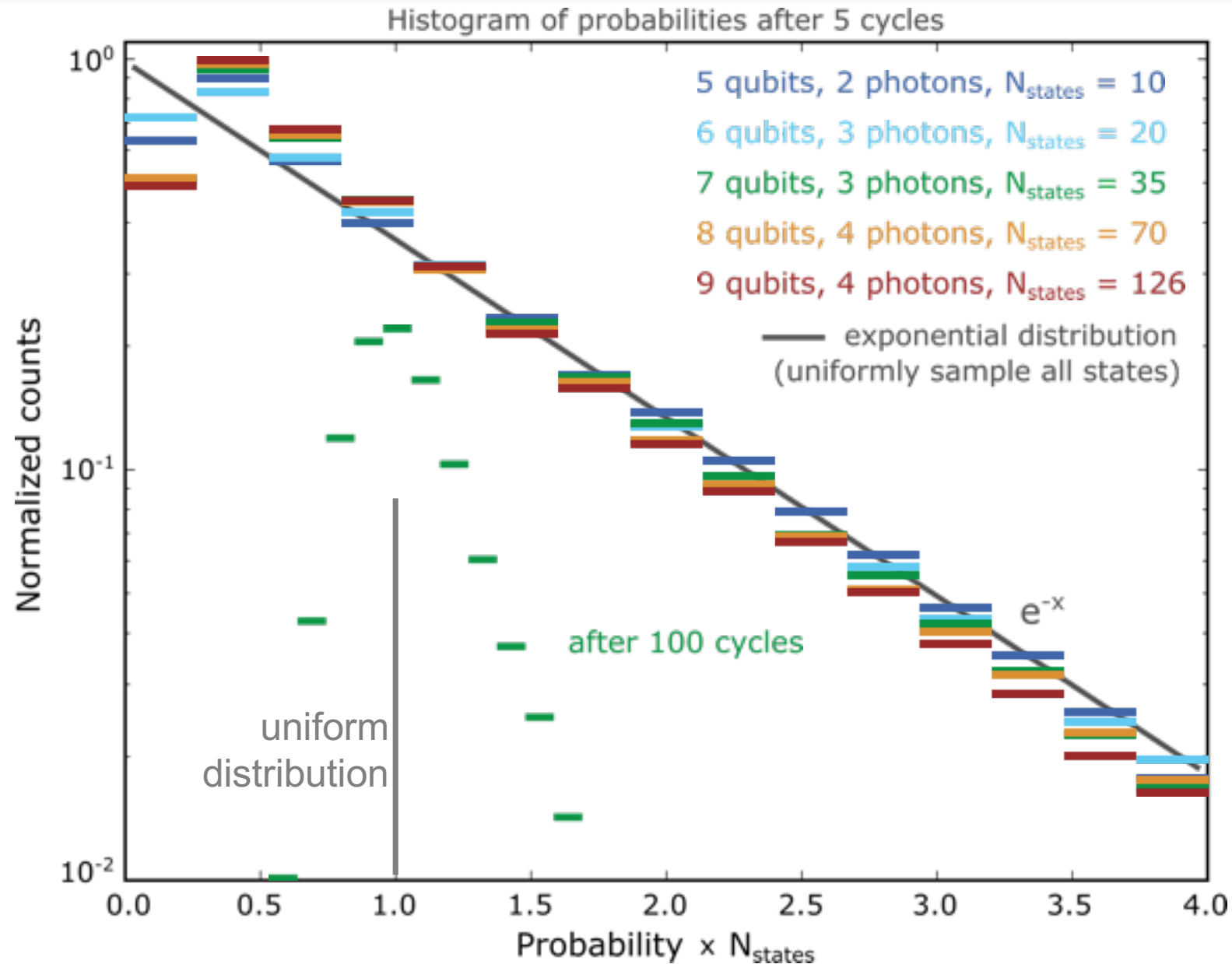


# Histogram of measured probabilities



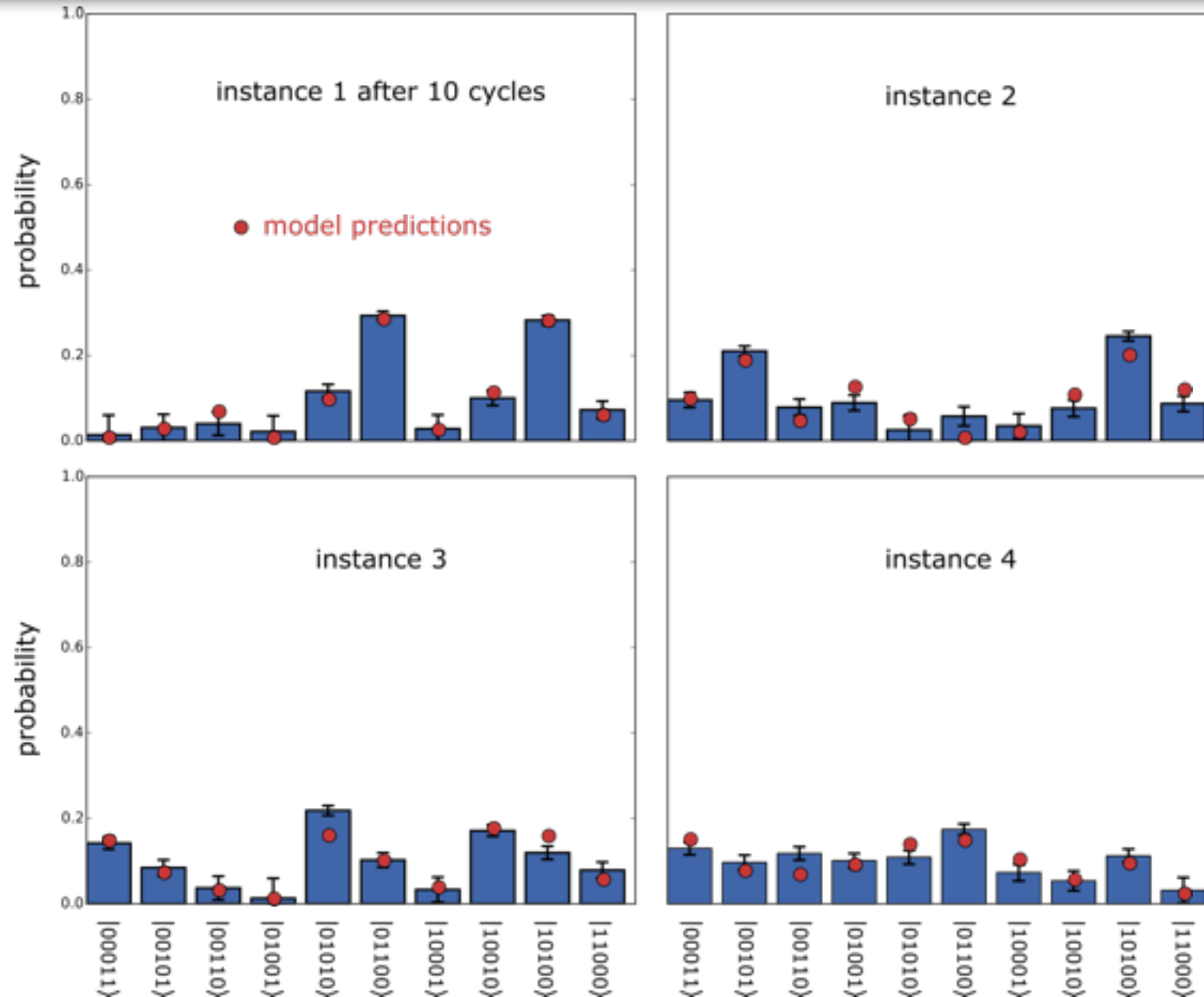
Collapses to  
exponential  
distribution

# Histogram of measured probabilities



decoherence kills  
qubit speckle

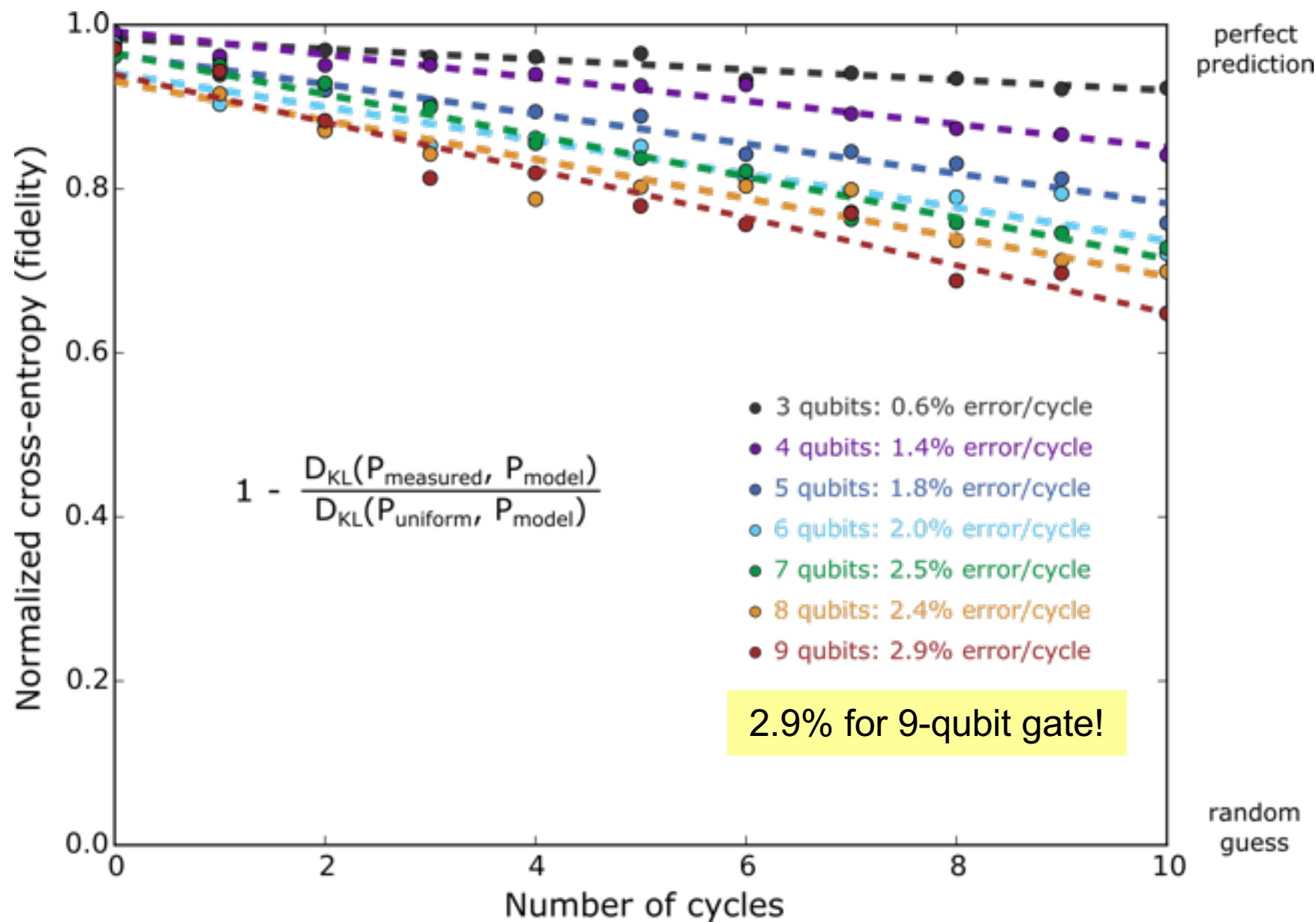
# Compare probabilities of experiment and theory



speckle pattern  
matches theory



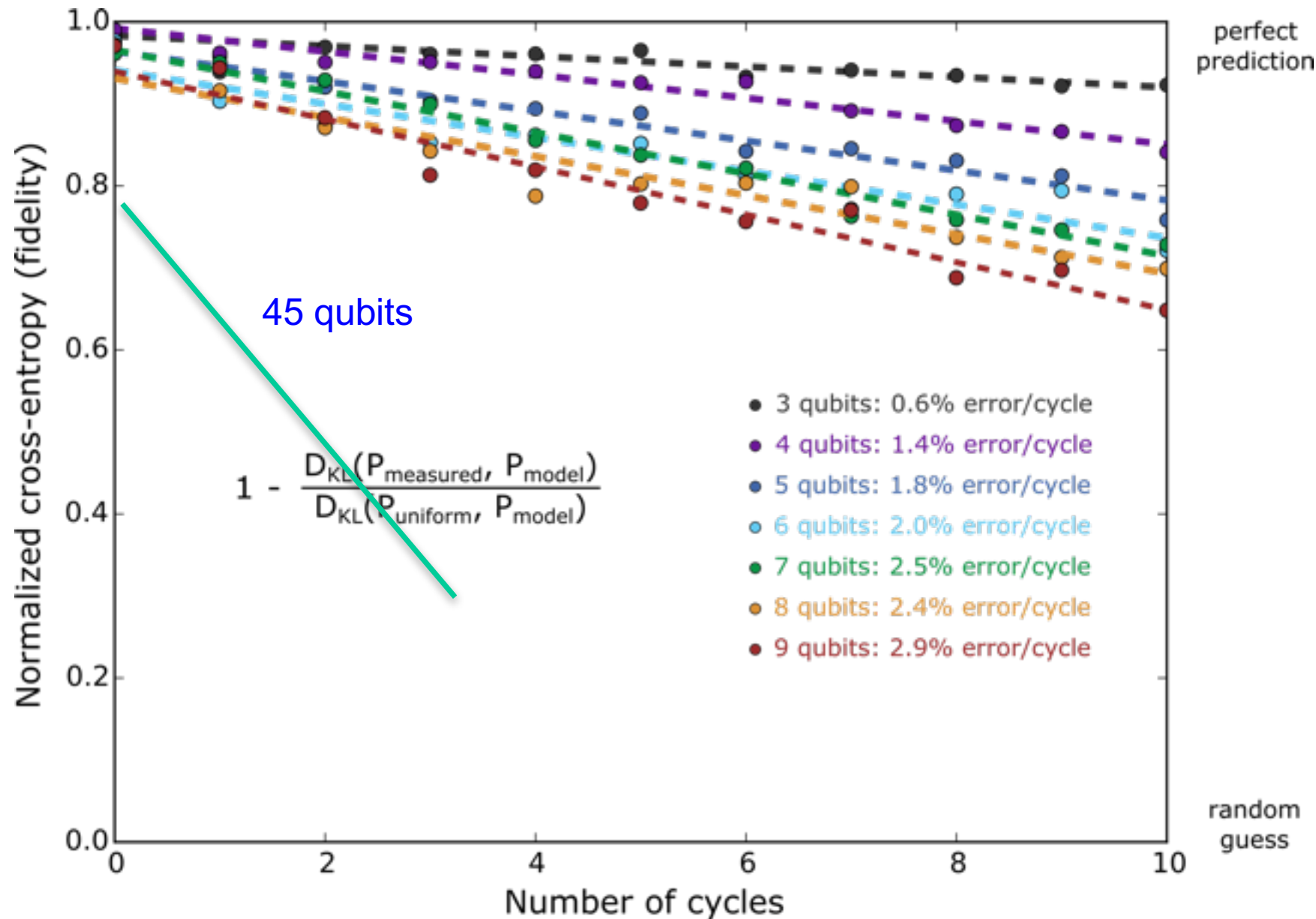
# Measuring fidelity



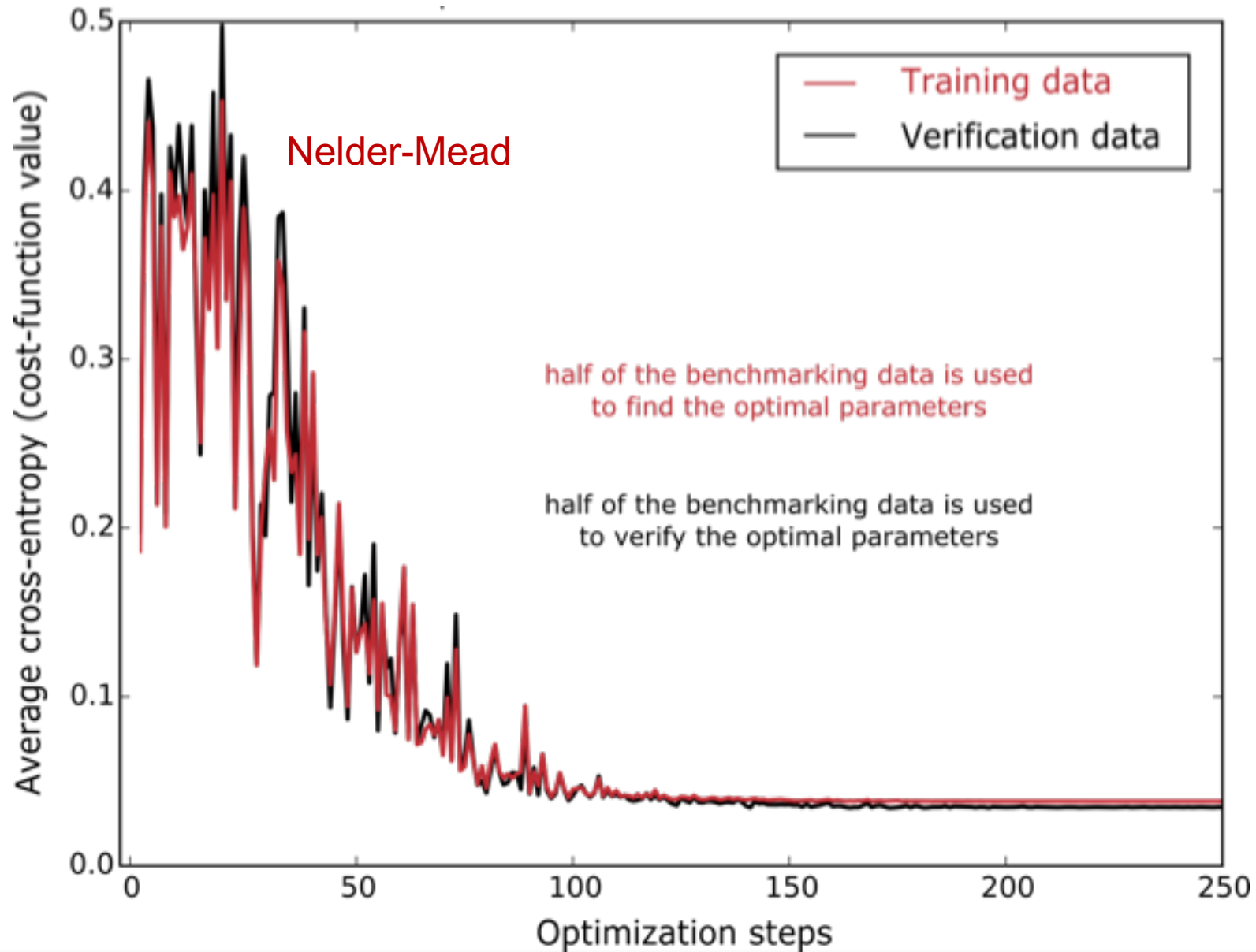
2.9% for 9-qubit gate!

0.3% error  
per gate & cycle

# Scaled fidelity for 45 qubits



# Useful: Learning a better control model



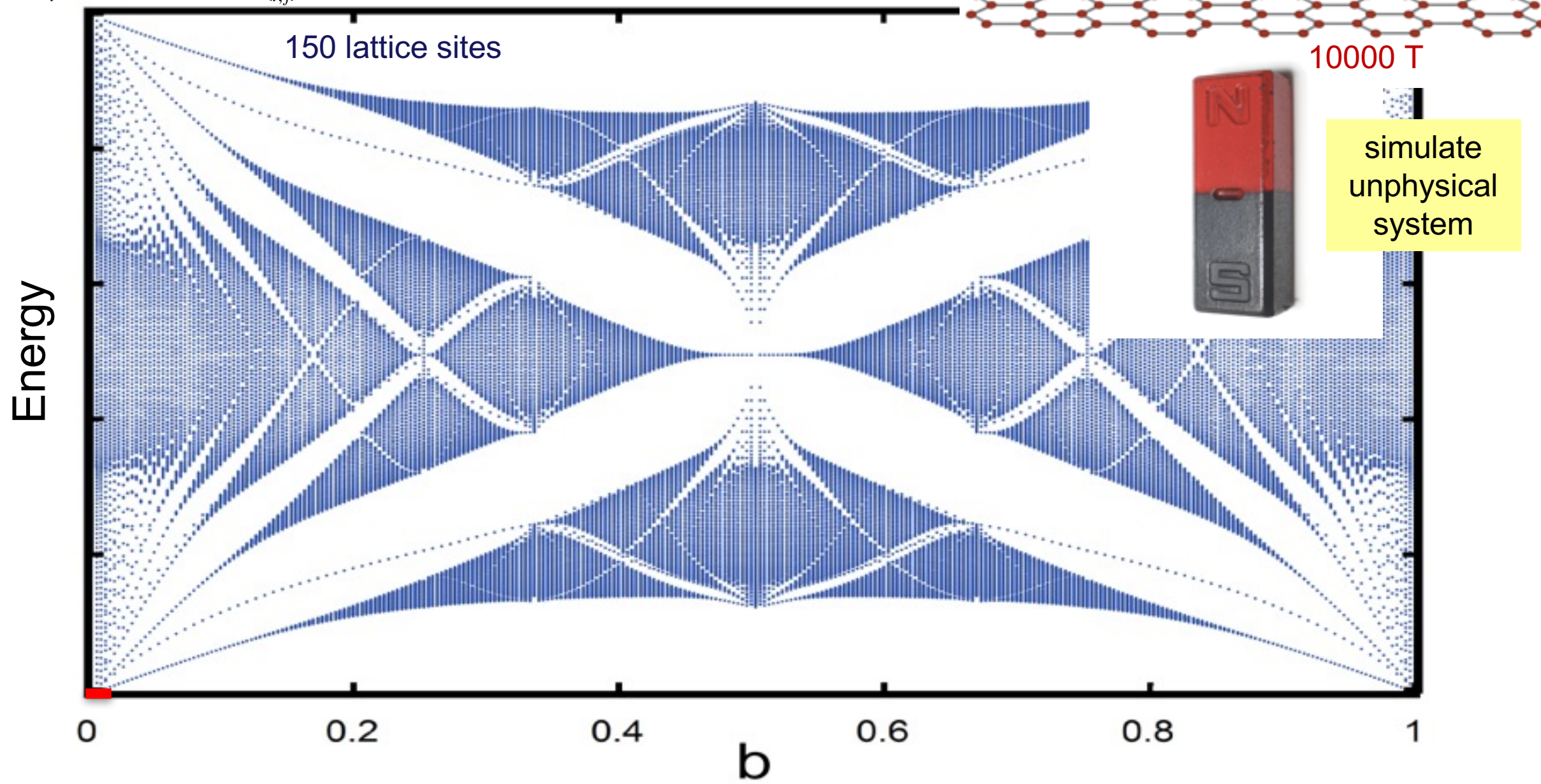
Tuneup flux offsets  
(as drifty)

training  
verified



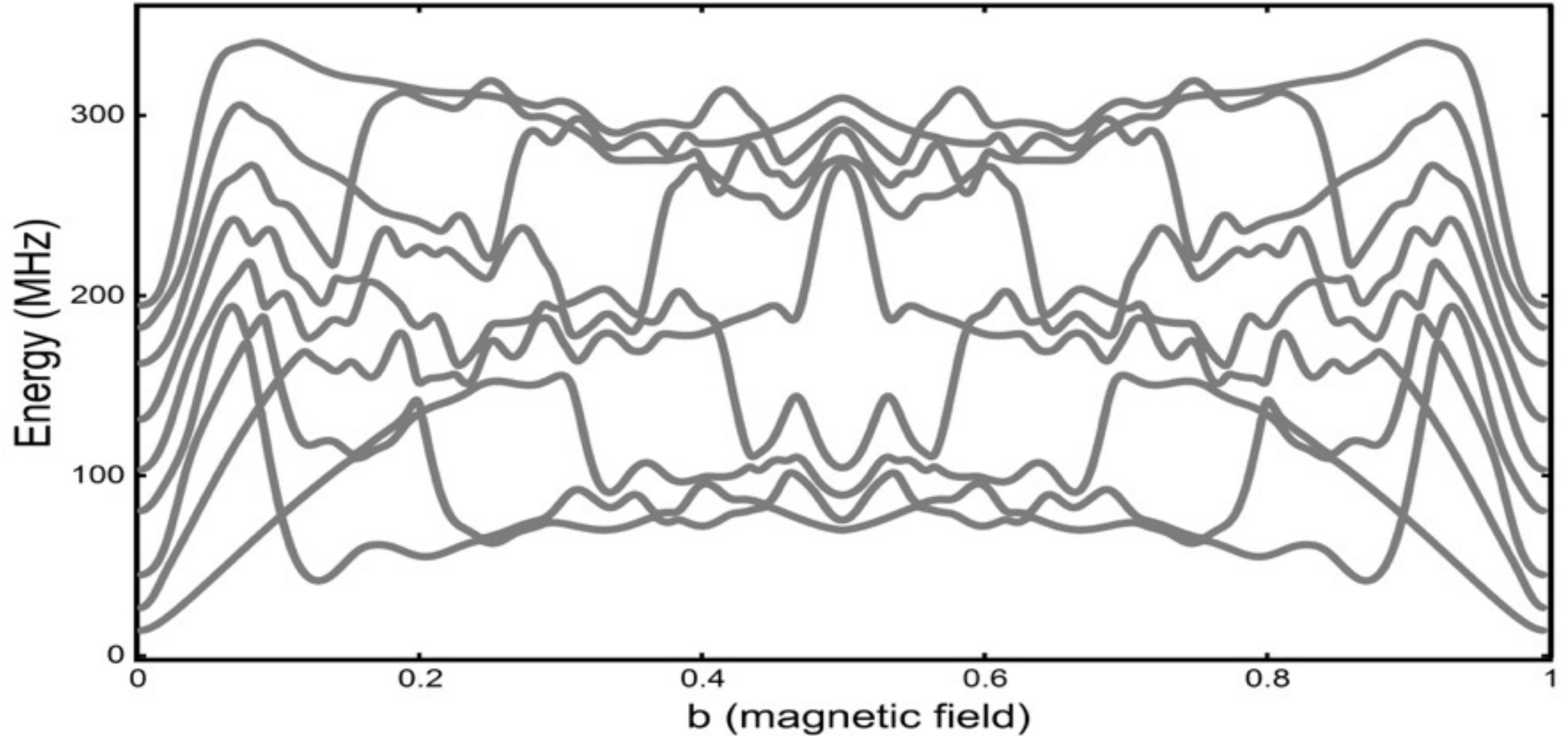
# Hofstadter Butterfly

$$H(b) = t \sum_i^{N_Q} \cos(2\pi i b) \sigma_i^Z + t \sum_{\langle i,j \rangle}^{N_Q-1} (\sigma_i^X \sigma_j^X + \sigma_i^Y \sigma_j^Y)$$



# 9 Qubits: theory

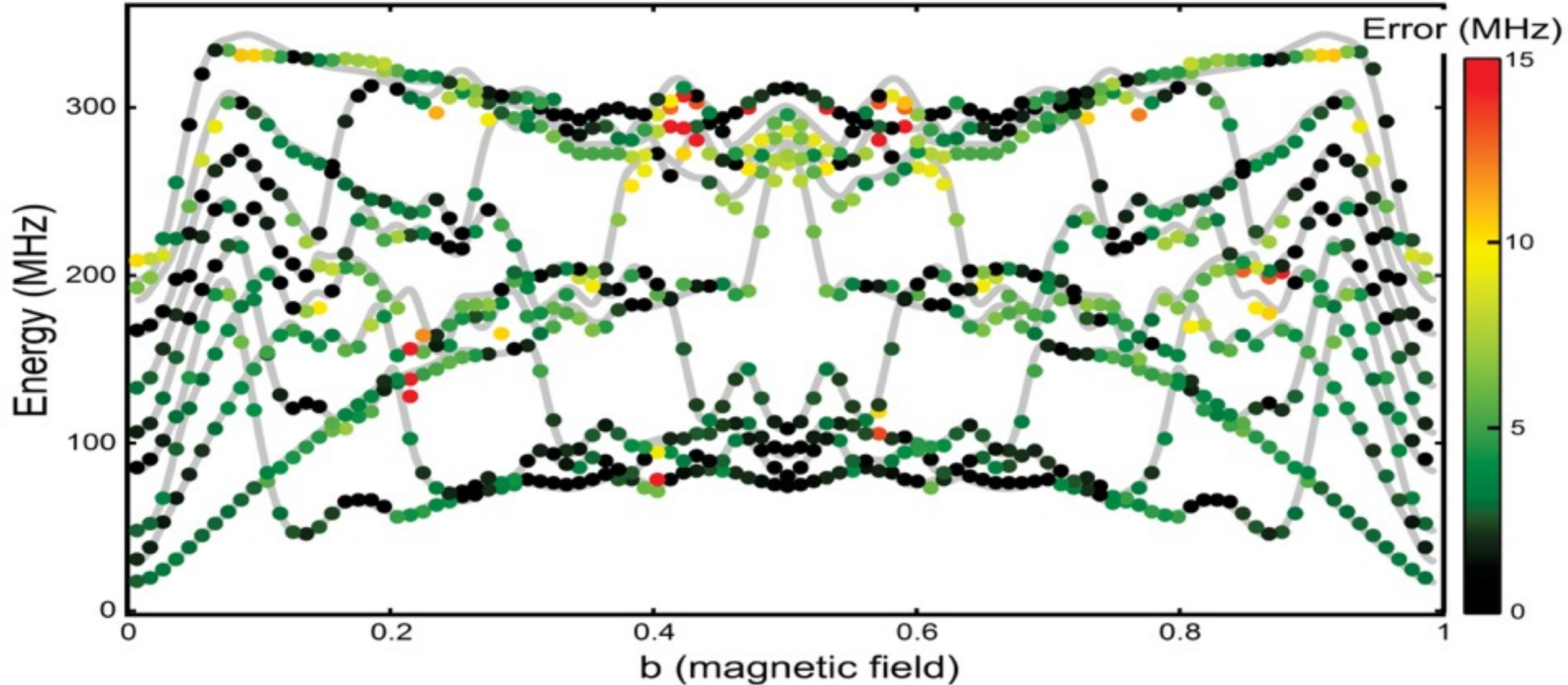
fractal nature gives  
complex spectrum





# 9 Qubits: theory + experiment

extract complex  
physically useful information





# More System Metrics

1) Quantity

2) Quality

2-qubit errors

Measure errors

1-qubit errors

3) Device speed

100,000 difference in technologies

Affects calibration

Affects \$/user

4) Qubit connectivity

2D array works for error correction ...

Serial (vs parallel) is slower

# Google Hardware Plans

## Quality

- 1) 9 qubit devices, both gate based and continuous (gmon)  
1 qubit: 0.05-0.1% error  
2 qubit 0.5-1%

- 2) 22 qubit device in test (2x11 array)  
Performance similar to 9 qubit device  
(better crosstalk)

## Quantity

- 3) Quantum supremacy device in fabrication  
Square array  
Testing in 2 weeks  
Working towards Quantum Cloud offering
- 4) Technology path scalable to 1000+ qubits



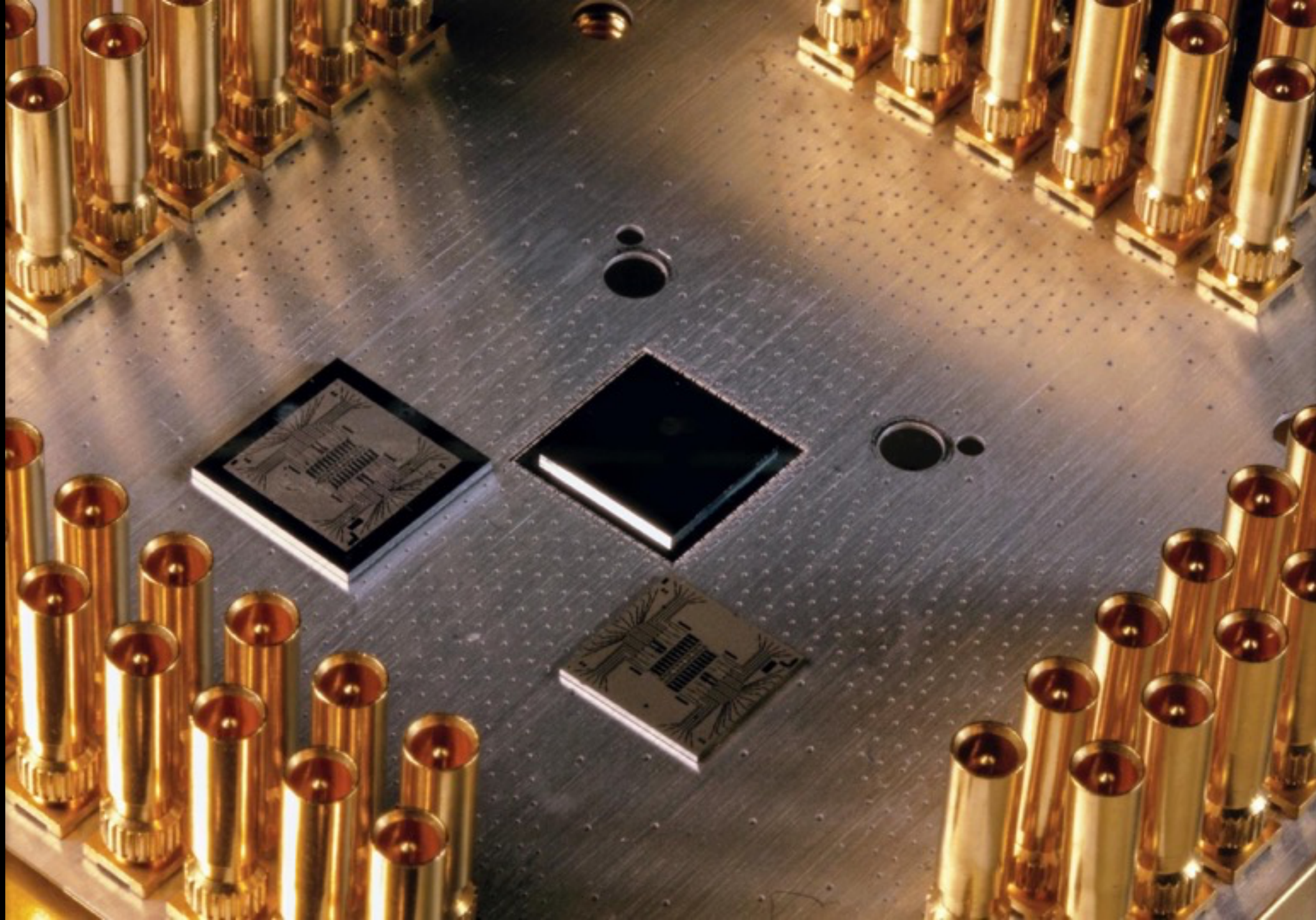
# Summary: Ask 3 Questions

1) Quantity and quality

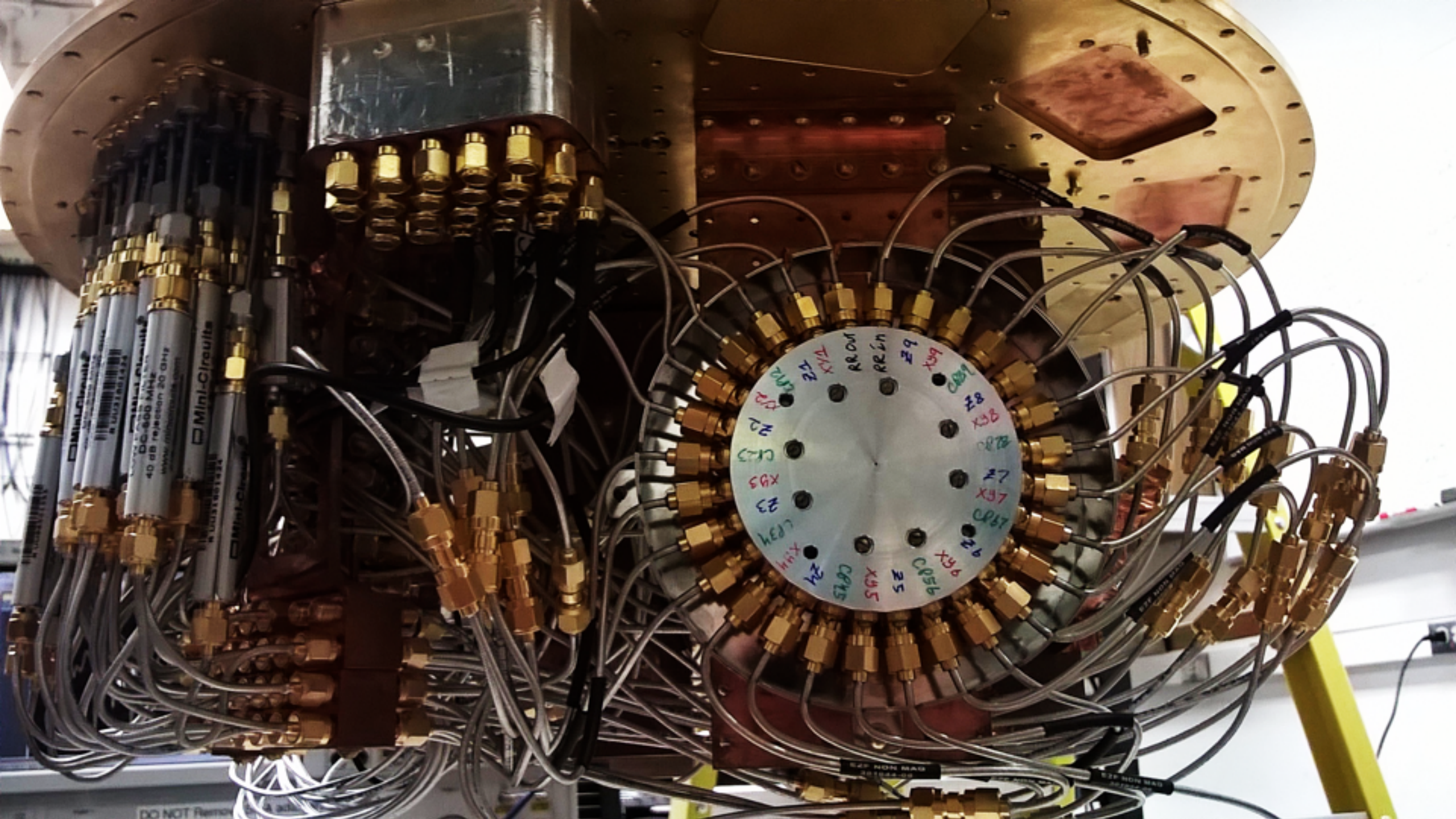
2) Quality(quantity)

3) Worst system error (2-qubit)

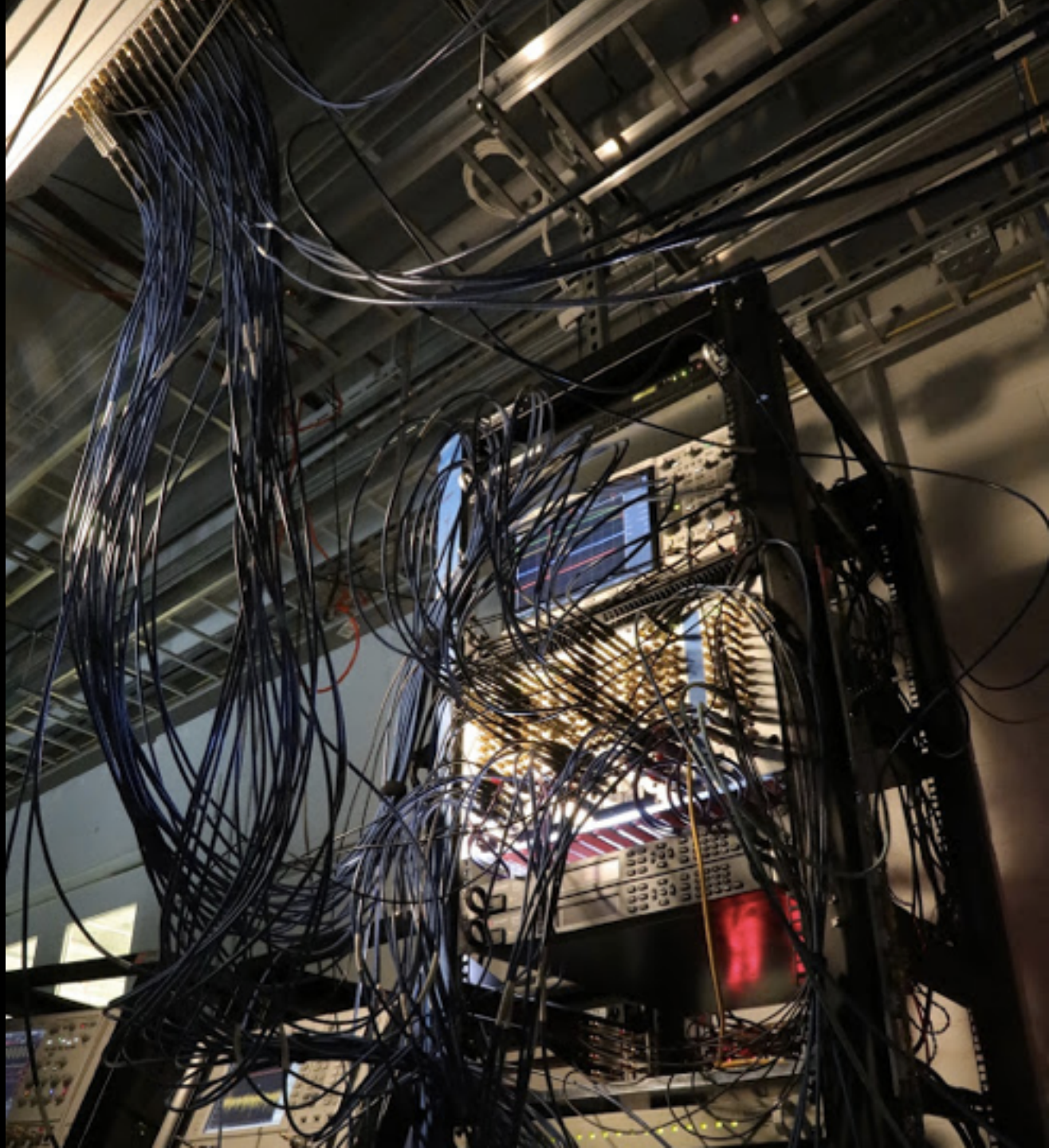
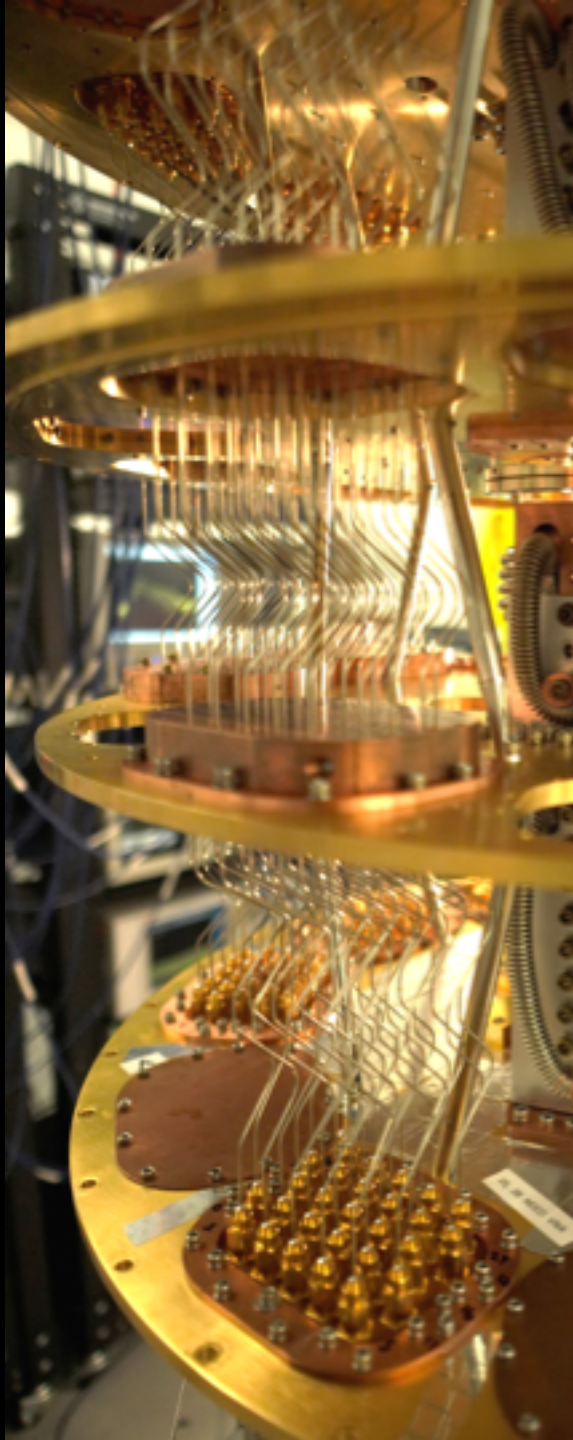








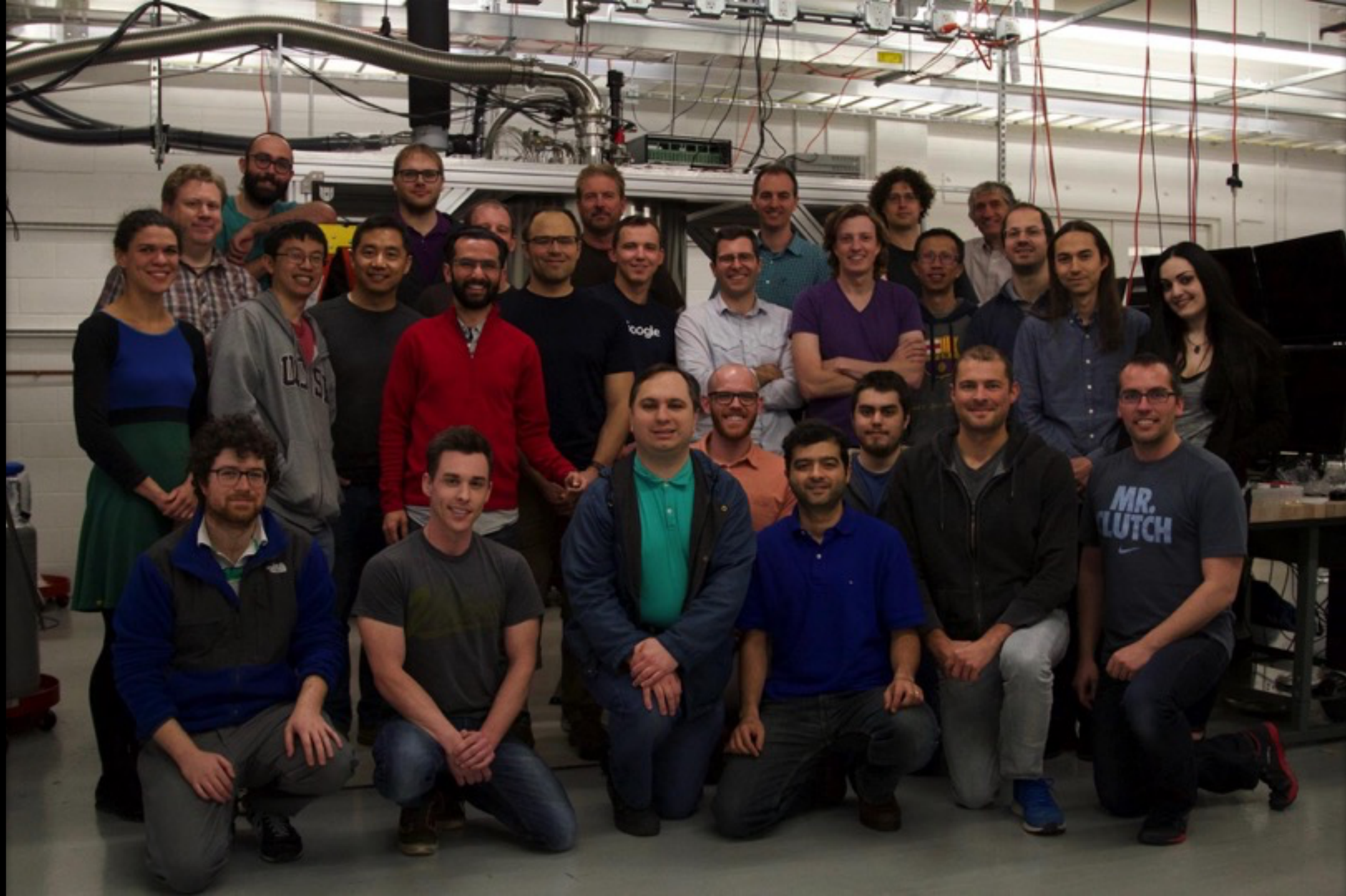






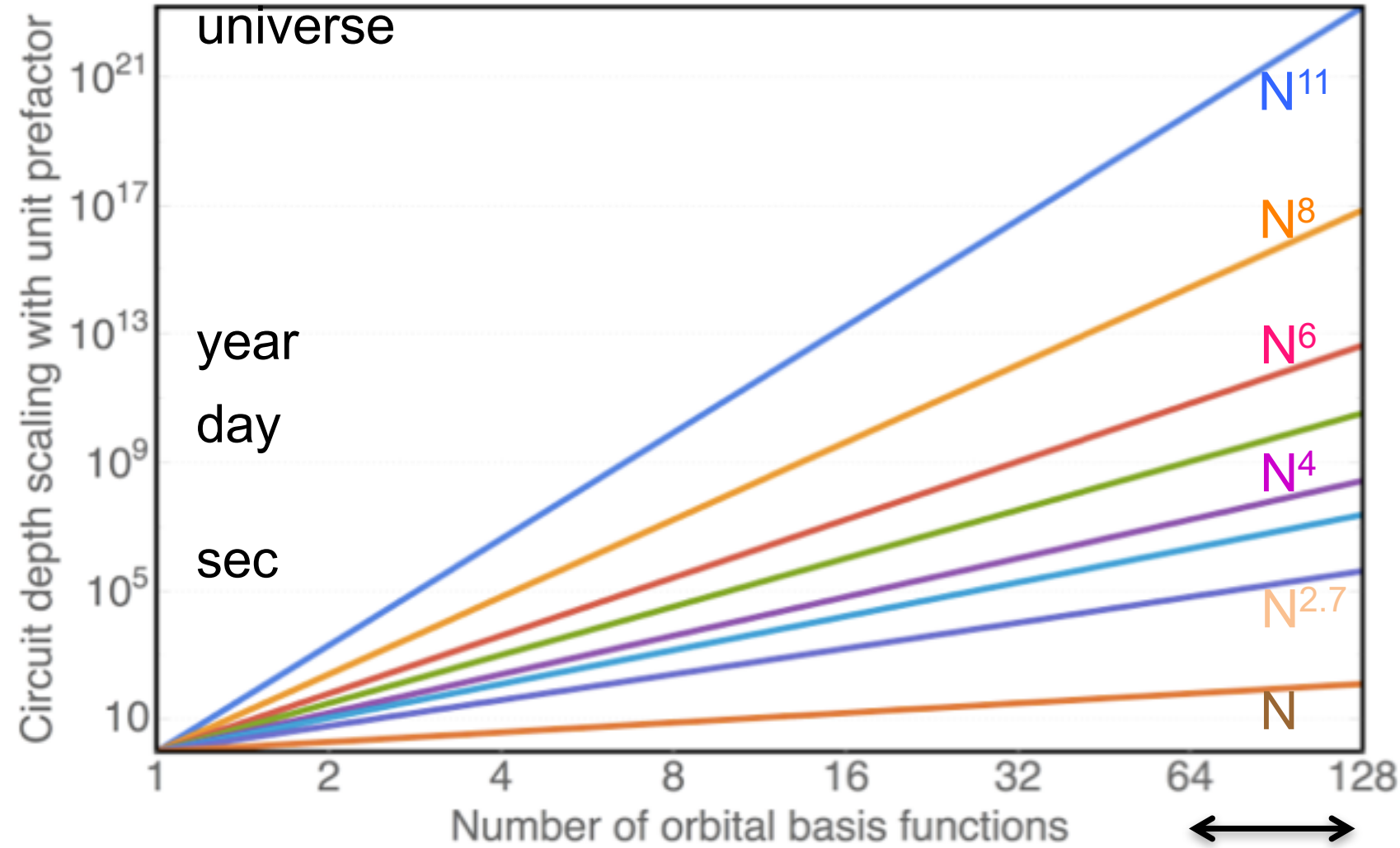






# Huge Progress in Algorithms (Quantum Chemistry)

Year	Reference	Total Depth
1985	Feynman	(proposal)
2005	Aspuru-Guzik [1]	$\mathcal{O}(\text{poly}(N))$
2010	Whitfield [2]	$\mathcal{O}(\text{poly}(N))$
2012	Seeley [3]	$\mathcal{O}(\text{poly}(N))$
2013	Perruzzo [4]	$\mathcal{O}(\text{poly}(N))$
2013	Toloui [5]	$\mathcal{O}(\text{poly}(N))$
2013	Wecker [6]	$\mathcal{O}(N^{11})$
2014	Hastings [7]	$\mathcal{O}(N^8)$
2014	Poulin [8]	$\sim N^6$
2014	McClean [9]	$\sim N^6$
2014	Babbush [10]	$\sim N^5$
2015	Babbush [11]	$\tilde{\mathcal{O}}(N^5)$
2015	Babbush [12]	$\tilde{\mathcal{O}}(\eta^2 N^3)$
2015	Wecker [13]	$\mathcal{O}(N^4)$
2016	McClean [14]	$\mathcal{O}(\eta^2 N^2)$
2017	Babbush [15]	$\mathcal{O}(\eta^{1.83} N^{1.67})$
2017	Babbush [15]	$\tilde{\mathcal{O}}(N^{2.67})$
2017	Babbush [15]	$\mathcal{O}(N)$



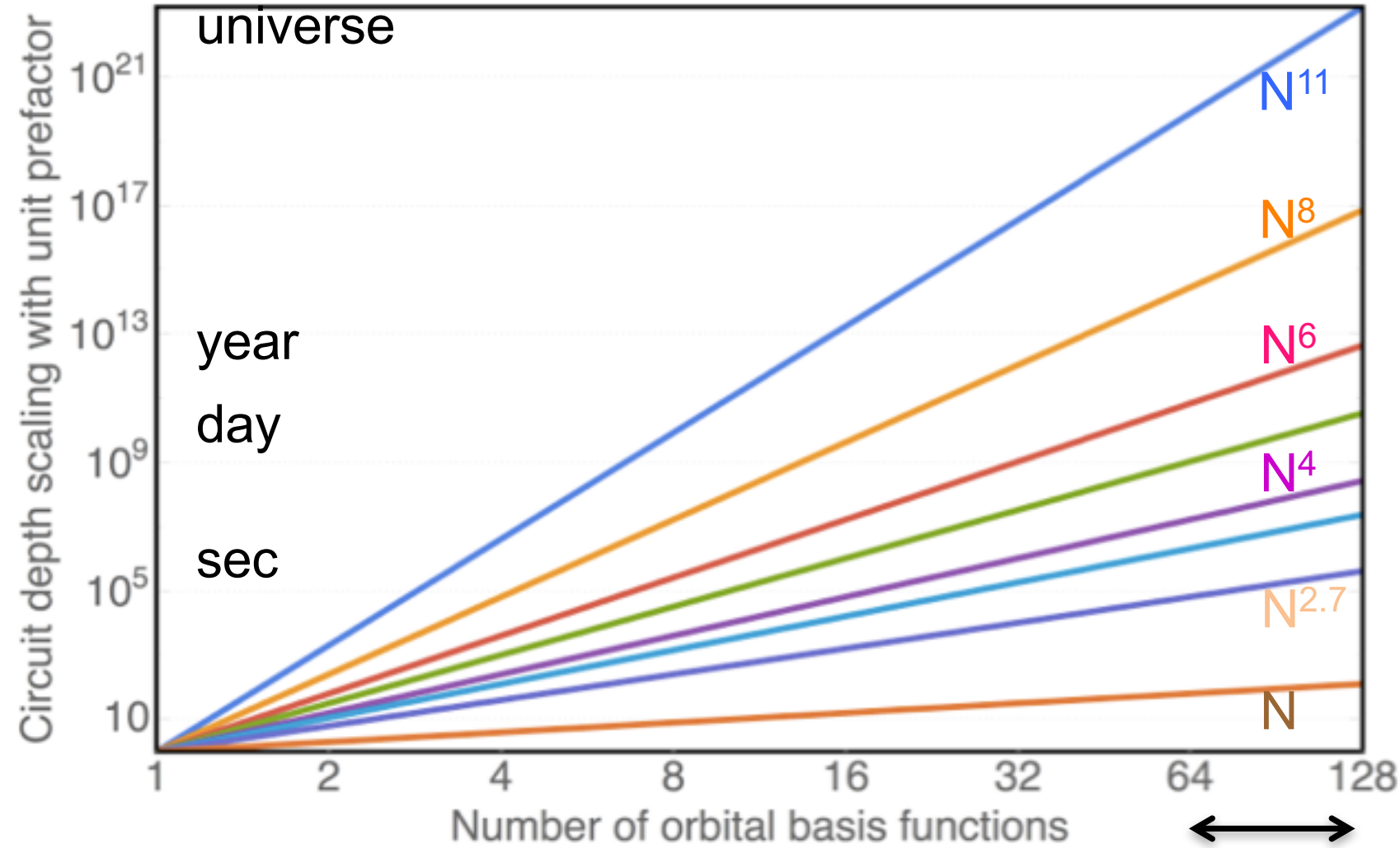
Exact: 100 logical qubits (error corrected)

Approximate: 100 physical qubits (?)



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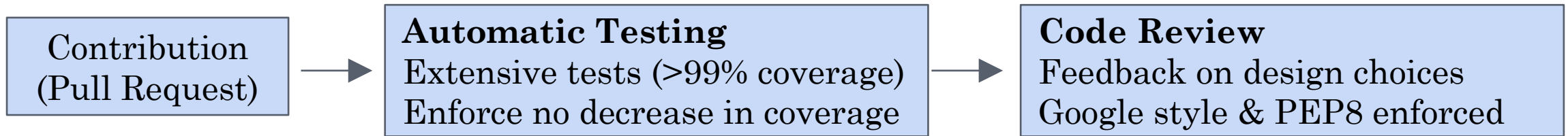
Useful QC now possible?

# OpenFermion: The Electronic Structure Package for Quantum Computers

## Open source library for quantum simulation of fermions

- Generate fermionic Hamiltonian from molecule geometry, charges, etc.
- Map fermions to qubits (e.g. Jordan-Wigner)
- Compile to a variety of gate sets

## Modern software engineering practices



## Framework and platform agnostic

- Works above LIQUID, ProjectQ, [insert your platform here]
- Runs on Windows, Mac, and Linux

## OpenFermion is a community effort!

- Submit your changes at [openfermion.org](https://openfermion.org)
- Collaborators include Google, Rigetti, NASA, Harvard, ETH Zurich, University of Michigan, Dartmouth, Oxford, the Department of Energy, ...

